



Rocket City Math League 2017-2018
Gemini Solutions Round 1

1. Answer: 100 units

Use Pythagorean Theorem to find the hypotenuse: $a^2 + b^2 = c^2$
 $28^2 + 96^2 = c^2$
 $784 + 9216 = c^2$
 $10,000 = c^2$
 $C = 100$ units

2. Answer: 13°

The sum of the interior angles for a triangle is 180.
 $38^\circ + 14^\circ - 2^\circ = 50^\circ$; $180^\circ - 50^\circ = 130^\circ$; $130^\circ = (3x + 7x)$; $130^\circ = 10x$; $x = 130^\circ / 10 = 13^\circ$

3. Answer: 259,200

Sum of all interior angles for regular polygon: $(180n - 360)^\circ$
Sum of all exterior angles for regular polygon is 360°
Sum of interior angles for a regular hexagon: $(180(6) - 360) = 720$
 $720 * 360 = 259,200$

4. Answer: 4,000,000π square miles

Surface Area of a Sphere Formula: $4\pi r^2$; plug in the radius value $4(\pi)(1,000)^2$;
leave answer in terms of π to get $4,000,000\pi^2$ miles.

5. Answer: 50π

Find the arc length for the side of the cake where frosting is missing.
Formula for arc length: $l = m/360 * C$
 l = length of arc, m = measure of arc, c = circumference
Circumference = $2\pi r$. $12(2)\pi = 24\pi$
Plug in variables: $l = (125/360) * 24\pi = 3000\pi/360$
Simplify: $25\pi/3$

Find the area of the region that needs to be re-frosted by multiplying the arc length by the height of the cake.

$$(25\pi/3) \times (6) = 150\pi/3 = 50\pi$$

6. Answer: 384cm

Divide the total area of the house by the number of square rooms to find the area of one room.

$$960/15 = 64$$
, then find the side length of each room by taking square root: $\sqrt{64} = 8$

Find the possible dimensions of the house: 3×5 , and 15×1

$$\text{Find the perimeter of the house with dimensions } 3 \times 5: 3(8) + 3(8) + 5(8) + 5(8) = 128$$

$$\text{Find the perimeter of the house with dimensions } 15 \times 1: 15(8) + 15(8) + 1(8) + 1(8) = 256$$

$$\text{Add the perimeters of both houses: } 128 + 256 = 384$$

7. Answer: 64/17

In the figure: $AD/AC = AC/AB$

Use Pythagorean Theorem to find AC: $x^2 + 15^2 = 17^2$; $x^2 + 225 = 289$

$$x^2 = 64$$
; $x = 8$; $AC = 8$

$$AD/8 = 8/17$$

Cross multiply and get: $17x = 64$

$$x = 64/17$$

8. Answer: 14,406.32 cm³ or 360158/25

Volume of a cylinder: $\pi r^2(h)$; r is the radius, and h is the height

Volume of a cone: $1/3\pi r^2(h)$; r is the radius, and h is the height

Subtract the volume of the cone from the volume of the cylinder.

$$\text{Plug in values: } (\pi 10^2(46)) - (1/3\pi 2^2(9))$$

$$((3.14)(100)(46)) - ((1/3)(3.14)(4)(9))$$

$$(14,444) - (37.68) = 14,406.32 \text{ cm}^3$$

9. Answer: 9

Radius of circumscribed circle about any angle:

$$R = \text{product of the sides} / 4(\text{area of the triangle})$$

Find the area of the triangle using Heron's formula: $\sqrt{s(s-a)(s-b)(s-c)}$

$$\text{Semi perimeter} = \text{perimeter} / 2 = (15 + 4 + 13) / 2 = 16$$

$$\sqrt{16(16-15)(16-4)(16-13)} = 24$$

$$R = (15 * 4 * 13) / 4(24) = (780) / (96) = 8.125 \text{ which rounds up to } 9$$

10. Answer: $\frac{105\sqrt{3}+52}{4}$ or $13 + \frac{105\sqrt{3}}{4}$

Use law of cosines to find side c: $c^2 = a^2 + b^2 - 2ab(\cos C)$

Plug in values: $c^2 = 7^2 + 15^2 - 2(7)(15)(\cos 60^\circ)$

$$c^2 = 49 + 225 - 210(1/2)$$

$$c^2 = 49 + 225 - 105 = 169; c = 13$$

Area of any triangle: $1/2ab(\sin C)$

$$(1/2)(7)(15)(\sin 60^\circ) = \frac{105\sqrt{3}}{4}$$

$$\text{Add side c and the area together: } 13 + \frac{105\sqrt{3}}{4} = \frac{105\sqrt{3} + 52}{4}$$